Domain-size-dependent exchange bias in Co/LaFeO$_3$

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X-ray microscopy using magnetic linear dichroism of a zero-field-grown multidomain Co/LaFeO$_3$ ferromagnet/antiferromagnet sample shows a local exchange bias of random direction and magnitude. A statistical analysis of the local bias of individual micron-size magnetic domains demonstrates an increasing bias field with decreasing domain size as expected for a random distribution of pinned, uncompensated spins, which are believed to mediate the interface coupling. A linear dependence with the inverse domain diameter is found. © 2004 American Institute of Physics. [DOI: 10.1063/1.1813633]

Exchange bias, the unidirectional pinning of the magnetization of a ferromagnet (FM) by an antiferromagnet (AFM), is the result of magnetic interface exchange coupling. Since the macroscopic magnetization of an antiferromagnet is compensated because of the balance of moment in all spin sublattices, it is widely accepted that breaking of the in-plane translational symmetry is required to explain bias, in particular on compensated AFM surfaces. This symmetry breaking can either be the result of interface roughness, of magnetic domains, defects, or of a combination of these four. Elaborate models have been developed describing many phenomena related to exchange bias, which consider one or more of these possible sources of bias. Common to most models is a randomness of the local bias due to the stochastic distribution of pinned uncompensated spins in the AFM that mediate the coupling. This randomness can lead to a strong lateral variation of the bias field. The existence of pinned uncompensated spins was experimentally observed by magnetometry, by x-ray dichroism, by magnetic force microscopy, and by nonlinear optical spectroscopy. It was also shown that the coupling strength scales with the number of pinned uncompensated spins and that it is inversely correlated with the grain size of a polycrystalline AFM. Such a scaling law was first discussed by Malozemoff in a random-field model. The underlying idea is that for a large statistical sample of domains with diameter $d$ and a total number of surface spins of $N \sim d^2$, the statistical deviation of the uncompensated magnetization from exact compensation is proportional to the standard deviation or width of a normal distribution: $\sqrt{N} \sim d$. The width of the bias distribution in such a model is proportional to the uncompensated moment per area $d^2$ and therefore $\sim 1/d$. In this letter, we will demonstrate that the local bias field of a large sample of domains is indeed normal distributed and that a $1/d$ scaling law describes the width of the bias distribution as function of domain diameter.

We studied a molecular-beam epitaxy-grown 1.2 nm Co/40 nm LaFeO$_3$ epitaxial thin film on a SrTiO$_3$(001) substrate. The sample preparation was described in Ref. 14. The experiments were conducted at the photoemission electron microscopy (PEEM)-2 microscope of the Advanced Light Source. The sample was neither field cooled nor field grown and therefore did not show macroscopic exchange bias. This allows us to study the undisturbed microscopic distribution of the unidirectional coupling. It was shown before that similar samples exhibit local bias. The (001) surface of antiferromagnetic LaFeO$_3$ is completely compensated with antiferromagnetic axes along out-of-plane $\langle 110 \rangle$ directions. The directions refer to the cubic lattice of the substrate. Interface coupling to the AFM and the magnetostatic field force the Co magnetization parallel to the in-plane projection of the local LaFeO$_3$ antiferromagnetic axis, parallel to $\langle \pm 100 \rangle$ or $\langle \pm 010 \rangle$. Magnetic domain images of Co using PEEM and x-ray magnetic circular dichroism (XMCD) show two classes of FM domains, Fig. 1. The FM domains are coupled 1:1 to AFM domains from white ($-223$ Oe) to black ($+223$ Oe), which possesses a uniaxial anisotropy parallel to $[100]$. The orthogonal $[010]$ domains remain unchanged (gray). Remanent hysteresis loops recorded from single domains show a bias field of random size and random direction. The loops were calculated from a sequence of Co XMCD images, acquired after applying field pulses of increasing magnitude (step 5 Oe).
Two typical loops of spatially close domains, which show opposite bias, are displayed in Fig. 1, bottom left. A map of the local bias field was generated by analyzing the local loops of all domains $i$ with area $A_i > 0.1 \mu m^2$, inset of Fig. 2. The local bias field $h_i$ was determined as the difference of the switching field measured with increasing positive and negative magnetic field. Domains along $[010]$, which did not switch, were masked out. The area of each domain was determined by an image analysis program. The bias map shows a wide variation of the local bias field of up to ±30 Oe. Both negative and positive values are present because no bias direction was set.

Three switching field cycles were measured on the same area to obtain switching data from a total of more than 1200 domains with minimum area above 0.1 $\mu m^2$. A crosscorrelation of 0.7 between bias maps of consecutive cycles demonstrated a generally reproducible local bias of individual domains. A domain was defined as a connected area that switched at the same field. The resolution limit of the microscope of 0.1 $\mu m$ was well below the minimum domain size that was considered in the analysis. The switching data as function of field and domain area is summarized in Fig. 2. The majority of the domains are below 2 $\mu m^2$ in area and a widening of the bias distribution for smaller domains is apparent. The data are normal distributed and are symmetrical to zero bias, in agreement with the prediction of the random-field approach. The standard deviation of the bias distribution can be written as $\sigma = \sqrt{\sum h_i^2}$ (the average bias vanishes), and it is a measure for the average absolute value of the bias. In order to statistically test or reject the hypothesis of a widening of the bias distribution we performed Bartlett’s test, which tests the hypothesis that two or more normal distributed samples have the same or different variance. We chose 400 domains each for two statistical samples, one containing the largest, the other the smallest domains. Bias field histograms and Gauss fits of these two statistical samples are shown at the top of Fig. 2. An increase of the standard deviation from 9.4 Oe for the largest to 14.1 Oe for the smallest domains was found. The test result of 64.7, compared to a much smaller $x^2$ critical value of 10.8 at a 99.9% confidence level, means that the hypothesis of equal variance has to be rejected. The increase in variance or width of the bias distribution with decreasing domain size is statistically significant according to Bartlett’s test.

The widening of the bias distribution as function of decreasing domain area is shown in Fig. 3. The total distribution was divided into 11 equal-sized groups of 115 domains, of which the standard deviation $\sigma$ of the bias field is plotted. The bunching of the data points at a low area is a result of the dominance of small domains in the distribution. The standard deviation starts at 7.9 Oe for, on average, 3.9 $\mu m^2$ domains and reaches 14.0 Oe for 0.11 $\mu m^2$ domains. Note, that because of the equal group size, all data points have approximately equal errors, the value of which can be discerned from the scatter of the bias data at a small domain area. More instructive is a plot of the standard deviation of the bias distribution as a function of $1/\sqrt{A}$ or the inverse diameter (Fig. 3, inset). The dependence is clearly linear over about a...
domains, however, have a higher chance of containing a significant surplus of pinned spins pointing in the same direction, which leads to local bias. When a sample is explicitly biased, e.g., by field cooling, then the center of the bias distribution is displaced from zero bias. A larger bias will be found on a sample containing predominantly small domains, which have, on average, a larger ratio between uncompensated spins and compensated spins.

In summary, we have studied the dependence of the standard deviation of the local bias field distribution with the domain area for Co/LaFeO$_3$(001). Using x-ray microscopy, we have determined microscopic maps of the bias field domain by domain, and have statistically analyzed the bias field distribution. The analysis shows a statistically significant increase of the width of the bias field distribution with decreasing domain area and an inverse dependence with the domain diameter. This functional dependence is the result of the stochastic nature of exchange bias.

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12NIST/SEAMECH e-Handbook of Statistical Methods.
13Both distributions have a mean bias not significantly different from zero, tested using a t test, and are fitted well by Gaussians, which are not constrained in width and position.